

SSC CGL (Tier – II) Mathematics Practice Set

Answers with Explanation

1. (c) Suppose that

$$1 + \frac{1}{10 + \frac{1}{10}} = \frac{111}{101} = a$$

শ্রুতিভঙ্গ

$$1 - \frac{1}{10 + \frac{1}{10}} = \frac{91}{101} = b$$

$$\therefore \frac{a^2 - b^2}{a + b} = \frac{(a + b)(a - b)}{(a + b)} = (a - b)$$

$$= \frac{111}{101} - \frac{91}{101} = \frac{20}{101}$$

2. (d) Check through options

$$\frac{1}{3 + \frac{1}{1 + \frac{1}{2 + \frac{1}{4}}}}$$

শ্রুতিভঙ্গ

$$= \frac{1}{3 + \frac{1}{1 + \frac{1}{\frac{8+1}{4}}}} = \frac{1}{3 + \frac{1}{1 + \frac{4}{9}}}$$

$$= \frac{1}{3 + \frac{1}{\frac{9+4}{9}}} = \frac{1}{3 + \frac{9}{13}} = \frac{1}{\frac{39+9}{13}} = \frac{13}{48}$$

3. (a) $\frac{1}{\sqrt{3.25} + \sqrt{2.25}}$

শ্রুতিভঙ্গ

$$= \frac{1}{\sqrt{3.25} + \sqrt{2.25}} \times \frac{\sqrt{3.25} - \sqrt{2.25}}{\sqrt{3.25} - \sqrt{2.25}}$$

$$= \frac{\sqrt{3.25} - \sqrt{2.25}}{3.25 - 2.25} = \sqrt{3.25} - \sqrt{2.25}$$

Similarly,

$$\frac{1}{\sqrt{4.25} + \sqrt{3.25}} = \sqrt{4.25} - \sqrt{3.25}$$

$$\frac{1}{\sqrt{5.25} + \sqrt{4.25}} = \sqrt{5.25} - \sqrt{4.25}$$

$$\frac{1}{\sqrt{6.25} + \sqrt{5.25}} = \sqrt{6.25} - \sqrt{5.25}$$

শ্রুতিভঙ্গ

\therefore Expression

$$= \sqrt{3.25} - \sqrt{2.25} + \sqrt{4.25} - \sqrt{3.25} + \sqrt{5.25} - \sqrt{4.25} + \sqrt{6.25} - \sqrt{5.25} \\ = \sqrt{6.25} - \sqrt{2.25} = 2.5 - 1.5 = 1$$

4. (c) $\frac{1}{\sqrt{3} + \sqrt{4}}$

$$= \frac{1}{\sqrt{3} + \sqrt{4}} \times \frac{\sqrt{4} - \sqrt{3}}{\sqrt{4} - \sqrt{3}}$$

$$= \frac{\sqrt{4} - \sqrt{3}}{4 - 3} = \sqrt{4} - \sqrt{3}$$

শ্রুতিভঙ্গ

Similarly,

$$= \frac{1}{\sqrt{4} + \sqrt{5}} = \sqrt{5} - \sqrt{4} \dots \text{so on}$$

\therefore Expression

$$= \sqrt{4} - \sqrt{3} + \sqrt{5} - \sqrt{4} + \sqrt{6} - \sqrt{5} + \sqrt{7} - \sqrt{6} + \sqrt{8} - \sqrt{7} + \sqrt{9} - \sqrt{8} \\ = \sqrt{9} - \sqrt{3} = 3 - \sqrt{3}$$

5. (a) $\frac{x^3 - y^3}{x^2 + xy + y^2} = \frac{5}{1}$

$$\Rightarrow \frac{(x - y)(x^2 + xy + y^2)}{x^2 + xy + y^2} = 5$$

$$\Rightarrow x - y = 5 \quad \dots (i)$$

Again,

$$\frac{x^2 - y^2}{x - y} = 7$$

শ্রুতিভঙ্গ

$$\Rightarrow \frac{(x + y)(x - y)}{x - y} = 7$$

$$\Rightarrow x + y = 7 \quad \dots (ii)$$

On adding equations (i) and (ii),

$$2x = 12 \Rightarrow x = 6$$

From equation (ii),

$$x + y = 7 \Rightarrow y = 7 - 6 = 1$$

$$\therefore \frac{2x}{3y} = \frac{2 \times 6}{3 \times 1} = 4 : 1$$

প্র্যাচিভর্স

6. (d) Since 18% of the students neither play football nor cricket. It means 82% of the students either play football or cricket or both.

Using set theory

$$\therefore n(A \cup B) = n(A) + n(B) - n(A \cap B)$$

$$\Rightarrow 82 = 40 + 50 - n(A \cap B)$$

$$\Rightarrow n(A \cap B) = 90 - 82 = 8$$

\therefore 8% students play both games.

7. (b) Using Rule 1,

Tricky Approach

If the cost price is ₹100, then selling price = ₹120 and gain = ₹20

$$\text{Required gain \%} = \frac{20}{120} \times 100 = \frac{50}{3} = 16\frac{2}{3}\%$$

8. (a) C.P. of 1 bucket = x

C.P. of 1 mug = y

প্র্যাচিভর্স

$$\therefore 8x + 5y = 92 \dots(i)$$

$$5x + 8y = 77 \dots(ii)$$

By using equation (i) \times 5 - equation (ii) \times 8,

$$40x + 25y - 40x - 64y$$

$$- 460 - 616$$

$$\Rightarrow -39y = - 156$$

$$\Rightarrow y = 4$$

From equation (i),

$$8x + 20 = 92$$

$$\Rightarrow 8x = 92 - 20 = 72$$

$$\Rightarrow x = 9$$

\therefore C.P. of 2 mugs and 3 buckets

$$= 2 \times 4 + 3 \times 9$$

$$= 8 + 27 = ₹35$$

প্র্যাচিভর্স

9. (c) Principal + S.I. for $\frac{5}{2}$ years = ₹1012 ... (i)

Principal + S.I. for 4 years = ₹1067.20 ... (ii)

Subtracting equation (i) from (ii)

$$\text{S.I. for } \frac{3}{2} \text{ years} = ₹55.20$$

$$\therefore \text{S.I. for } \frac{5}{2} \text{ years} = 55.20 \times \frac{2}{3} \times \frac{5}{2} = ₹92$$

$$\therefore \text{Principal} = ₹(1012 - 92) = ₹920$$

$$\therefore \text{Rate} = \frac{92 \times 100}{920 \times \frac{5}{2}} = \frac{92 \times 100}{920 \times \frac{5}{2}}$$

$$= \frac{2 \times 92 \times 100}{920 \times 5} = 4\%$$

10. (b) P = ₹3000, A = ₹3993, n = 3 years

$$A = P \left(1 + \frac{r}{100} \right)^n$$

প্র্যাচিভর্স

$$\therefore \left(1 + \frac{r}{100} \right)^n = \frac{A}{P}$$

$$\left(1 + \frac{r}{100} \right)^3 = \frac{3993}{3000} = \frac{1331}{1000}$$

$$\left(1 + \frac{r}{100} \right)^3 = \left(\frac{11}{10} \right)^3$$

$$\Rightarrow 1 + \frac{r}{100} = \frac{11}{10}$$

$$\Rightarrow \frac{r}{100} = \frac{11}{10} - 1$$

$$\Rightarrow \frac{r}{100} = \frac{1}{10} \Rightarrow r = \frac{100}{10}$$

$$\therefore r = 10\%$$

প্র্যাচিভর্স

11. (c) $x = \sqrt{\frac{\sqrt{5}+1}{\sqrt{5}-1}} \times \frac{\sqrt{5}+1}{\sqrt{5}+1} = \sqrt{\frac{(\sqrt{5}+1)^2}{5-1}}$

$$= \sqrt{\frac{(\sqrt{5}+1)^2}{4}} = \frac{\sqrt{5}+1}{2}$$

$$\therefore 5x^2 - 5x - 1$$

$$= 5 \left(\frac{(\sqrt{5}+1)}{2} \right)^2 - 5 \frac{(\sqrt{5}+1)}{2} - 1$$

$$= 5 \left(\frac{5+1+2\sqrt{5}}{4} \right) - \frac{5\sqrt{5}+5}{2} - 1$$

$$= 5 \left(\frac{3+\sqrt{5}}{2} \right) - \frac{5\sqrt{5}+5}{2} - 1$$

$$= \frac{15+5\sqrt{5}-5\sqrt{5}-5-2}{2} = \frac{8}{2} = 4$$

প্র্যাচিভর্স

12. (c) $4A + \frac{7}{B} + 2C + \frac{5}{D} + 6E = 47.2506$

$$= 40 + 7 + \frac{2}{10} + \frac{5}{100} + \frac{6}{10000}$$

$$4A = 40 \Rightarrow A = 10$$

$$\frac{7}{B} = 7 \Rightarrow 7B = 7 \Rightarrow B = 1$$

$$2C = \frac{2}{10} \Rightarrow C = 0.1$$

$$\frac{5}{D} = \frac{5}{100} \Rightarrow D = 100$$

$$6E = \frac{6}{10000} \Rightarrow E = 0.0001$$

$$\begin{aligned} 5A + 3B + 6C + D + 3E \\ = 5 \times 10 + 3 \times 1 + 6 \times 0.1 + 100 + \\ 3 \times 0.0001 \\ = 50 + 3 + 0.6 + 100 + 0.0003 = 153.6003 \end{aligned}$$

$$13. (c) \frac{2p}{p^2 - 2p + 1} = \frac{1}{4}$$

$$\Rightarrow \frac{p^{2+} - 2p + 1}{2p} = 4$$

$$\Rightarrow \frac{p^2 - 2p + 1}{p} = 8$$

$$\Rightarrow \frac{p^2}{p} - \frac{2p}{p} + \frac{1}{p} = 8$$

$$\Rightarrow p + \frac{1}{p} = 8 + 2 = 10$$

$$14. (c) \frac{1}{\operatorname{cosec}^2 51^\circ} + \sin^2 39^\circ + \tan^2 51^\circ$$

$$\begin{aligned} - \frac{1}{\sin^2 51^\circ \cdot \sec^2 39^\circ} \\ = \sin^2 51^\circ + \sin^2 39^\circ + \tan^2(90^\circ - 39^\circ) - \end{aligned}$$

$$\begin{aligned} - \frac{1}{\sin^2(90^\circ - 39^\circ) \cdot \sec^2 39^\circ} \\ = \cos^2 39^\circ + \sin^2 39^\circ + \cot^2 39^\circ - \end{aligned}$$

$$\begin{aligned} \frac{1}{\cos^2 39^\circ \cdot \sec^2 39^\circ} \\ [\because \sin(90^\circ - \theta) = \cos \theta \\ \tan(90^\circ - \theta) = \cot \theta] \\ = 1 + \cot^2 39^\circ - 1 \\ = \operatorname{cosec}^2 39^\circ - 1 = x^2 - 1 \end{aligned}$$

$$15. (c) \frac{\frac{3}{2}}{\frac{1}{2}} \div \frac{4}{7} \left(\frac{4+3}{10} \right) \text{ of } \frac{\frac{3+2}{6}}{\frac{3-2}{6}}$$

$$= 3 \div \frac{4}{7} \left(\frac{7}{10} \right) \text{ of } \left(\frac{5}{6} \times 6 \right)$$

$$= 3 \div \left(\frac{4}{7} \times \frac{7}{10} \times 5 \right) = 3 \div 2 = \frac{3}{2}$$

$$16. (b) \text{ Let } 0.03 = x \Rightarrow 0.003 = \frac{x}{10}$$

$$0.21 = y \Rightarrow 0.021 = \frac{y}{10}$$

$$\text{and } 0.065 = z \Rightarrow 0.0065 = \frac{z}{10}$$

\(\therefore\) Expression

$$\begin{aligned} &= \sqrt{\frac{x^2 + y^2 + z^2}{\left(\frac{x}{10}\right)^2 + \left(\frac{y}{10}\right)^2 + \left(\frac{z}{10}\right)^2}} \\ &= \sqrt{100 \frac{(x^2 + y^2 + z^2)}{(x^2 + y^2 + z^2)}} = \sqrt{100} = 10 \end{aligned}$$

$$17. (a) (64)^{\frac{-2}{3}} \times \left(\frac{1}{4}\right)^{-2}$$

$$= \frac{1}{(64)^{\frac{2}{3}}} \times (4)^2$$

$$= \frac{1}{(4)^{3 \times \frac{2}{3}}} \times 4^2 = \frac{1}{4^2} \times 4^2 = 1$$

$$18. (c) \left[\left(\sqrt[5]{x^{-3/5}} \right)^{\frac{-5}{3}} \right]^5$$

$$= \left(x^{-\frac{3}{5}} \right)^{\frac{1}{5} \times \frac{-5}{3} \times 5}$$

$$= x^{-\frac{3}{5} \times \frac{-5}{3}} = x$$

$$19. (b) A : B = 5 : 4 = 45 : 36$$

$$B : C = 9 : 10 = 36 : 40$$

$$\therefore A : B : C = 45 : 36 : 40$$

Sum of the terms of ratio

$$= 45 + 36 + 40 = 121$$

$$\therefore C\text{'s share} = ₹ \left(\frac{40}{121} \times 2420 \right) = ₹ 800$$

20. (a) Let numbers = $5x$ and $4x$

$$\therefore 5x \times \frac{40}{100} = 12$$

$$\Rightarrow 2x = 12 \Rightarrow x = 6 \text{ and}$$

$$\text{Second number} = 6 \times 4 = 24$$

$$\therefore 50\% \text{ of } 24 = 24 \times \frac{50}{100} = 12$$

21. (a) $(A+B) \times \frac{40}{100}$

$$= (A-B) \times \frac{60}{100}$$

$$\Rightarrow 2(A+B) = 3(A-B)$$

$$\Rightarrow 2A + 2B = 3A - 3B$$

$$\Rightarrow A = 5B$$

$$\therefore \frac{2A-3B}{A+B} = \frac{10B-3B}{5B+B} = \frac{7B}{6B} = \frac{7}{6}$$

22. (c) After taking away respective balls,

Number of balls in the box

$$= 75 + 25 + 50 = 150$$

\therefore Percentage of black balls

$$= \frac{50}{150} \times 100 = \frac{100}{3} = 33\frac{1}{3}\%$$

23. (c) C.P. of watch = Rs. x (let)

$$\therefore \text{S.P.} = \frac{120x}{100} = ₹ \frac{6x}{5}$$

Case II

$$\text{C.P.} = ₹ \frac{9x}{10}$$

$$\text{S.P.} = ₹ \left(\frac{6x}{5} - 30 \right)$$

According to the question,

$$\frac{6x}{5} - 30 = \frac{9x}{10} \times \frac{120}{100} = \frac{27x}{25}$$

$$\Rightarrow \frac{6x}{5} - \frac{27x}{25} = 30$$

$$\Rightarrow \frac{30x - 27x}{25} = 30$$

$$\Rightarrow 3x = 30 \times 25$$

$$\Rightarrow x = \frac{30 \times 25}{3} = ₹ 250$$

24. (c) Let the C.P. of cycle be ₹ x .

Case I,

$$\text{S.P. of cycle} = ₹ \left(\frac{90x}{100} \right) = ₹ \frac{9x}{10}$$

Case II,

$$106\% \text{ of } x = \frac{9x}{10} + 200$$

$$\Rightarrow \frac{106x}{100} - \frac{9x}{10} = 200$$

$$\Rightarrow \frac{106x - 90x}{100} = 200$$

$$\Rightarrow \frac{16x}{100} = 200$$

$$\Rightarrow x = \frac{200 \times 100}{16} = ₹ 1250$$

25. (b) Principal = $\frac{\text{S.I.} \times 100}{\text{Time} \times \text{Rate}}$

$$= \frac{1 \times 100}{\frac{1}{365} \times 5} = \frac{365 \times 100}{5}$$

$$= ₹ 7300$$

26. (c) $\frac{1}{4} \times \frac{2}{6} \times \frac{3}{8} \times \frac{4}{10} \times \frac{5}{12} \dots \times \frac{31}{64} = \frac{1}{2^x}$

$$\Rightarrow \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} \times \dots \text{ to } 30 \text{ terms} \times \frac{1}{64} = \frac{1}{2^x}$$

$$\Rightarrow \frac{1}{2^{30}} \times \frac{1}{2^6} = \frac{1}{2^x}$$

$$\Rightarrow \frac{1}{2^{36}} = \frac{1}{2^x} \Rightarrow x = 36$$

27. (a) $\frac{a}{2} = \frac{b}{3} = \frac{c}{5} = k$ (Let)

$$\therefore a = 2k, b = 3k, c = 5k$$

$$\therefore \frac{a+b+c}{c} = \frac{2k+3k+5k}{5k} = \frac{10k}{5k} = 2$$

28. (b) $\frac{\sqrt{7}-2}{\sqrt{7}+2} = \frac{\sqrt{7}-2}{\sqrt{7}+2} \times \frac{\sqrt{7}-2}{\sqrt{7}-2}$

Rationalising the denominator)

$$= \frac{(\sqrt{7}-2)^2}{7-4} = \frac{7+4-4\sqrt{7}}{3}$$

$$= \frac{11}{3} - \frac{4\sqrt{7}}{3}$$

প্র্যাচিভর্স

প্র্যাচিভর্স

প্র্যাচিভর্স

প্র্যাচিভর্স

প্র্যাচিভর্স

প্র্যাচিভর্স

$$\therefore \frac{\sqrt{7}-2}{\sqrt{7}+2} = a\sqrt{7} + b$$

$$\Rightarrow \frac{11}{3} - \frac{4}{3}\sqrt{7} = a\sqrt{7} + b$$

Clearly,

$$a = -\frac{4}{3} \text{ and } b = \frac{11}{3}$$

প্র্যাক্টিস

29. (a) Let the rate of CI be R per cent per annum.

$$\therefore \text{CI} = P \left[\left(1 + \frac{R}{100} \right)^T - 1 \right]$$

$$\Rightarrow 5044 = 32000 \left[\left(1 + \frac{R}{400} \right)^3 - 1 \right]$$

[∵ Interest is compounded quarterly]

$$\Rightarrow \frac{5044}{32000} = \left(1 + \frac{R}{400} \right)^3 - 1$$

$$\Rightarrow \left(1 + \frac{R}{400} \right)^3 - 1 = \frac{1261}{8000}$$

প্র্যাক্টিস

$$\Rightarrow \left(1 + \frac{R}{400} \right)^3 = 1 + \frac{1261}{8000}$$

$$\Rightarrow \left(1 + \frac{R}{400} \right)^3 = \frac{1261}{8000} \left(\frac{21}{20} \right)^3$$

$$\Rightarrow 1 + \frac{R}{400} = \frac{21}{20} \Rightarrow \frac{R}{400} = \frac{21}{20} - 1 = \frac{1}{20}$$

$$\Rightarrow R = \frac{400}{20} = 20$$

30. (b) $\sin 17^\circ = \frac{x}{y}$

$$\cos 17^\circ = \sqrt{1 - \sin^2 17^\circ}$$

প্র্যাক্টিস

$$= \sqrt{1 - \frac{x^2}{y^2}} = \sqrt{\frac{y^2 - x^2}{y^2}}$$

$$= \frac{\sqrt{y^2 - x^2}}{y}$$

$$\therefore \sec 17^\circ = \frac{y}{\sqrt{y^2 - x^2}}$$

$$\sin 73^\circ = \sin (90^\circ - 17^\circ)$$

$$= \cos 17^\circ$$

$$\therefore \sec 17^\circ = \frac{1}{\sin 73^\circ}$$

$$= \frac{y}{\sqrt{y^2 - x^2}} = \frac{\sqrt{y^2 - x^2}}{y}$$

$$= \frac{y^2 - y^2 + x^2}{y\sqrt{y^2 - x^2}} = \frac{x^2}{y\sqrt{y^2 - x^2}}$$

প্র্যাক্টিস

31. (c) Suppose the C.P. of each article is ₹ 1

Then C.P. of 10 articles = ₹ 10

S.P. of 10 articles = ₹ 15

∴ Profit = ₹ 5

$$\% \text{ profit} = \frac{5 \times 100}{10} = 50\%$$

32. (d) C.P. of 100 oranges = ₹ 350

S.P. of 12 oranges = ₹ 48

$$\therefore \text{S.P. of 100 oranges} = \frac{48}{12} \times 100 = ₹ 400$$

Profit = ₹ (400 - 350) = ₹ 50

$$\therefore \text{Profit \%} = \frac{50}{350} \times 100 = \frac{100}{7} = 14\frac{2}{7}\%$$

33. (a) Expression

প্র্যাক্টিস

$$= \sqrt{5 + \sqrt{11 + \sqrt{19 + \sqrt{29 + 7}}}}$$

$$= \sqrt{5 + \sqrt{11 + \sqrt{19 + 6}}}$$

$$= \sqrt{5 + \sqrt{11 + 5}}$$

$$= \sqrt{5 + 4} = \sqrt{9} = 3$$

34. (a) The orders of the given surds are 3, 2, 4 and 6.

Their LCM = 12

Now we convert each surd into a surd of order 12.

$$\sqrt[3]{9} = (9)^{\frac{1}{3}} = (9)^{\frac{4}{12}} = (9^4)^{\frac{1}{12}} = \sqrt[12]{6561}$$

Similarly,

প্র্যাক্টিস

$$\sqrt{3} = \sqrt[12]{3^6} = \sqrt[12]{729}$$

$$\sqrt[4]{16} = \sqrt[12]{16^3} = \sqrt[12]{4096}$$

$$\sqrt[6]{80} = \sqrt[12]{80^2} = \sqrt[12]{6400}$$

Clearly,

$$\sqrt[12]{729} < \sqrt[12]{4096} < \sqrt[12]{6400} < \sqrt[12]{6561}$$

∴ $\sqrt[3]{9}$ is the greatest number.

35. (a) Third number = 100
 First number = 70
 Second number = 63
 ∴ Required percentage
 $= \frac{7}{70} \times 100 = 10$

36. (a) Rate = $\frac{S.I. \times 100}{\text{Principal} \times \text{Time}}$
 $= \frac{280 \times 100}{400 \times 10} = 7\%$ per annum

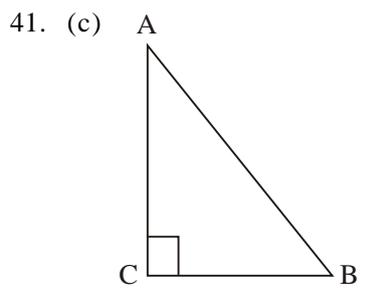
37. (b) $4^{4x+1} = \frac{1}{64} = \frac{1}{4^3}$
 $\Rightarrow 4^{4x+1} = 4^{-3}$
 $\Rightarrow 4x + 1 = -3$
 $\Rightarrow 4x = -4$
 $\Rightarrow x = -1$

38. (b) $\sqrt{1 - \frac{x^3}{100}} = \frac{3}{5}$
 Squaring both sides,
 $1 - \frac{x^3}{100} = \frac{9}{25}$
 $\Rightarrow \frac{x^3}{100} = 1 - \frac{9}{25} = \frac{25-9}{25} = \frac{16}{25}$
 $\Rightarrow x^3 = \frac{16}{25} \times 100 = 64$
 $\therefore x = \sqrt[3]{64} = \sqrt[3]{4 \times 4 \times 4} = 4$

39. (c) $x = (\sqrt{2} + 1)^{\frac{1}{3}}$
 $\Rightarrow x^{-3} = \sqrt{2} + 1$
 $\Rightarrow \frac{1}{x^3} = \sqrt{2} + 1$
 and $x^3 = \frac{1}{\sqrt{2} + 1} = \frac{1(\sqrt{2} - 1)}{(\sqrt{2} + 1)(\sqrt{2} - 1)} = \sqrt{2} - 1$
 $\therefore x^3 - \frac{1}{x^3}$
 $= \sqrt{2} - 1 - \sqrt{2} - 1 = 2$

40. (b) $\tan \theta = \frac{3}{4}$
 $\therefore \cot \theta = \frac{4}{3}$

$\therefore \operatorname{cosec}^2 \theta - \cot^2 \theta = 1$
 $\Rightarrow \operatorname{cosec} \theta = \sqrt{1 + \cot^2 \theta}$
 $= \sqrt{1 + \left(\frac{4}{3}\right)^2} = \sqrt{1 + \frac{16}{9}} = \sqrt{\frac{25}{9}} = \frac{5}{3}$



AC = BC = 5 cm
 $\therefore AB = \sqrt{AC^2 + BC^2}$
 $= \sqrt{5^2 + 5^2} = \sqrt{50} = 5\sqrt{2}$ cm

42. (d) Expression
 $= \sqrt{3 \frac{33}{64}} \div \sqrt{9 \frac{1}{7}} \times 2 \sqrt{3 \frac{1}{9}}$
 $= \sqrt{\frac{225}{64}} \div \sqrt{\frac{64}{7}} \times 2 \sqrt{\frac{28}{9}}$
 $= \sqrt{\frac{225}{64} \times \frac{7}{64} \times \frac{28}{9}} \times 2$
 $= \frac{5 \times 7}{8 \times 4} \times 2 = \frac{35}{16} = 2 \frac{3}{16}$

43. (b) $\sqrt[3]{9} - \sqrt[3]{3} + 1 = (3)^{\frac{2}{3}} - (3)^{\frac{1}{3}} + (1)^{\frac{2}{3}}$
 $\therefore (\sqrt[3]{3} + 1)(\sqrt[3]{9} - \sqrt[3]{3} + 1) = (3^{\frac{1}{3}})^3 + 1$
 $= 3 + 1 = 4$
 $\therefore a^3 + b^3 = (a + b)(a^2 - ab + b^2)$
 \therefore Rationalising factor = $\sqrt[3]{3} + 1$

44. (a) Let man's salary be x .
 \therefore His expenditure on items of daily use
 $= \frac{25}{2}\%$ of x
 $= \frac{25 \times x}{200} = \frac{x}{8}$
 So, remaining amount

প্র্যাচিভর্স

প্র্যাচিভর্স

প্র্যাচিভর্স

প্র্যাচিভর্স

প্র্যাচিভর্স

প্র্যাচিভর্স

$$= x - \frac{x}{8} = ₹ \frac{7x}{8}$$

Expenditure on house rent

$$= 30\% \text{ of } ₹ \frac{7x}{8}$$

$$= \frac{30}{100} \times \frac{7x}{8} = ₹ \frac{21x}{80}$$

Now, remaining amount

$$= \frac{7x}{8} - \frac{21x}{80}$$

$$= \frac{70x - 21x}{80} = ₹ \frac{49x}{80}$$

According to the question,

$$\therefore \frac{49x}{80} = 2940$$

$$\Rightarrow x = \frac{2940 \times 80}{49} = ₹ 4800$$

45. (b) C.P. of each article = $\frac{2400}{80} = ₹ 30$

Profit = 16%

\therefore S.P. of each article

$$= ₹ \left(\frac{30 \times 116}{100} \right) = ₹ 34.80$$

46. (a) Using Rule 1,
Let the cost price = $5x$ and the selling price = $6x$.

$$\text{Gain \%} = \frac{6x - 5x}{5x} \times 100 = 20\%$$

47. (d) Using Rule 1,
Let P be the principal and $R\%$ rate of interest.

$$\therefore \text{S.I.} = \frac{PR \times 10}{100} = \frac{PR}{10}$$

According to the question

$$\frac{PR}{10} = \left(P + \frac{PR}{10} \right) \times \frac{2}{5}$$

$$\Rightarrow \frac{R}{10} = \left(1 + \frac{R}{10} \right) \times \frac{2}{5}$$

$$\Rightarrow \frac{R}{10} = \frac{2}{5} + \frac{R}{25}$$

$$\Rightarrow \frac{R}{10} - \frac{R}{25} = \frac{2}{5}$$

$$\Rightarrow \frac{5R - 2R}{50} = \frac{2}{5}$$

$$\Rightarrow \frac{3R}{50} = \frac{2}{5}$$

$$\Rightarrow R = \frac{50 \times 2}{3 \times 5} = \frac{20}{3} = 6\frac{2}{3}\%$$

48. (c) Using Rule 1,
Principal (P) = Rs. S
Rate (R) = $2r\%$ per annum

$$\therefore \text{Amount} = P \left(1 + \frac{R}{100} \right)^T$$

$$= S \left(1 + \frac{2r}{100} \right)^3 = S \left(1 + \frac{r}{50} \right)^3$$

49. (b) Given $x = \frac{\sqrt{3}}{2}$

Given expression

$$= \frac{\sqrt{1+x}}{1+\sqrt{1+x}} + \frac{\sqrt{1-x}}{1-\sqrt{1-x}}$$

$$= \frac{\sqrt{1+x}}{1+\sqrt{1+x}} \times \frac{1-\sqrt{1+x}}{1-\sqrt{1+x}} + \frac{\sqrt{1-x}}{1-\sqrt{1-x}} \times \frac{1+\sqrt{1-x}}{1+\sqrt{1-x}}$$

$$= \frac{\sqrt{1+x}-1-x}{1-1-x} + \frac{\sqrt{1-x}+1-x}{1-1+x}$$

$$= \frac{\sqrt{1-x}+1-x}{x} - \frac{\sqrt{1+x}-1-x}{x}$$

$$= \frac{\sqrt{1-x}+1-x-\sqrt{1+x}+1+x}{x}$$

$$= \frac{2+\sqrt{1-x}-\sqrt{1+x}}{x}$$

$$= \frac{2+\sqrt{1-\frac{\sqrt{3}}{2}}-\sqrt{1+\frac{\sqrt{3}}{2}}}{\frac{\sqrt{3}}{2}}$$

$$= \frac{2+\sqrt{\frac{2-\sqrt{3}}{2}}-\sqrt{\frac{2+\sqrt{3}}{2}}}{\frac{\sqrt{3}}{2}}$$

অ্যাপ্রিভিউ

অ্যাপ্রিভিউ

অ্যাপ্রিভিউ

অ্যাপ্রিভিউ

অ্যাপ্রিভিউ

অ্যাপ্রিভিউ

$$= \frac{2 + \frac{\sqrt{4-2\sqrt{3}}}{2} - \frac{\sqrt{4+2\sqrt{3}}}{2}}{\frac{\sqrt{3}}{2}}$$

$$\left[\because \sqrt{4-2\sqrt{3}} = \sqrt{3+1-2\sqrt{3}} = \sqrt{(\sqrt{3}-1)^2} = \sqrt{3}-1 \right]$$

and

$$\begin{aligned} \left[\sqrt{4+2\sqrt{3}} = \sqrt{3+1+2\sqrt{3}} \right. \\ \left. = \sqrt{(\sqrt{3}+1)^2} = \sqrt{3}+1 \right] \\ = \frac{4 + \sqrt{3} - 1 - \sqrt{3} - 1}{\sqrt{3}} = \frac{2}{\sqrt{3}} \end{aligned}$$

শ্রীচিড়ার্স

50. (a) Third proportional of a and b = $\frac{b^2}{a}$

$$= \frac{(\sqrt{x^2+y^2})^2}{\frac{x}{y} + \frac{y}{x}} = \frac{x^2+y^2}{\frac{x^2+y^2}{xy}} = xy$$

শ্রীচিড়ার্স

51. (d) $\frac{x}{a} = \frac{1}{a} - \frac{1}{x}$

$$\begin{aligned} \Rightarrow \frac{x}{a} &= \frac{x-a}{ax} \\ \Rightarrow x^2 &= x-a \\ \Rightarrow x-x^2 &= a \end{aligned}$$

52. (c) $\frac{\sin\theta + \cos\theta}{\sin\theta - \cos\theta} = \frac{5}{4}$

$$\Rightarrow \frac{\cos\theta \left(\frac{\sin\theta}{\cos\theta} + 1 \right)}{\cos\theta \left(\frac{\sin\theta}{\cos\theta} - 1 \right)} = \frac{5}{4}$$

শ্রীচিড়ার্স

$$\begin{aligned} \Rightarrow \frac{\tan\theta + 1}{\tan\theta - 1} &= \frac{5}{4} \\ \Rightarrow 4\tan\theta + 4 &= 5\tan\theta - 5 \\ \Rightarrow \tan\theta &= 9 \\ \Rightarrow \frac{2\tan\theta}{2} &= \frac{5+4}{5-4} \end{aligned}$$

(By componendo and dividendo)

$$\begin{aligned} \therefore \frac{\tan^2\theta + 1}{\tan^2\theta - 1} &= \frac{(9)^2 + 1}{(9)^2 - 1} = \frac{81+1}{81-1} \\ &= \frac{82}{80} = \frac{41}{40} \end{aligned}$$

53. (a) a = 64 and b = 289

$$\therefore \sqrt{a} = \sqrt{64} = 8 \text{ and } \sqrt{b} = \sqrt{289} = 17$$

শ্রীচিড়ার্স

$$\begin{aligned} \therefore \left(\sqrt{\sqrt{a} + \sqrt{b}} - \sqrt{\sqrt{b} - \sqrt{a}} \right)^{\frac{1}{2}} \\ = \left(\sqrt{8+17} - \sqrt{17-8} \right)^{\frac{1}{2}} \\ = \left(\sqrt{25} - \sqrt{9} \right)^{\frac{1}{2}} \\ = (5-3)^{\frac{1}{2}} = (2)^{\frac{1}{2}} \end{aligned}$$

54. (b) $\left[\sqrt[3]{6\sqrt{5^9}} \right]^4 \left[\sqrt[6]{3\sqrt{5^9}} \right]^4$

$$\begin{aligned} = \left[5^{9 \times \frac{1}{6} \times \frac{4}{3}} \right]^4 \left[5^{9 \times \frac{1}{6} \times \frac{4}{3}} \right]^4 \\ = \left[5^{\frac{1}{2} \times 4} \right] \left[5^{\frac{1}{2} \times 4} \right] = 5^2 \times 5^2 = 5^4 \end{aligned}$$

শ্রীচিড়ার্স

55. (b) Number of brown socks = x

Price of brown socks = ₹y per pair
Price of black socks = ₹2y per pair
₹ 4y + x × 2y

$$= \frac{150}{100} (4 \times 2y + xy)$$

$$\Rightarrow 4 + 2x = \frac{3}{2}(8 + x)$$

$$\Rightarrow 8 + 4x = 24 + 3x$$

$$\Rightarrow x = 24 - 8 = 16$$

∴ Required ratio = 4 : 16 = 1 : 4

56. (d) Salary of clerk in 1974

$$= \frac{3600 \times 100}{100 + 20} = ₹3050$$

শ্রীচিড়ার্স

57. (b) Average price of blended tea

$$= \frac{280 \times 7 + 240 \times 9}{16}$$

$$= \frac{1960 + 2160}{16}$$

$$= \frac{4120}{16} = ₹ 257.50 \text{ kg}$$

58. (b) Required percent

$$= \left(35 - 20 - \frac{35 \times 20}{100} \right) \% = 8\%$$

59. (b) Rate = R% per annum

$$\therefore \text{Time} = \frac{R}{2} \text{ Years}$$

$$\therefore \text{Rate} = \frac{\text{S.I.} \times 100}{\text{Principal} \times \text{Time}}$$

$$\Rightarrow R = \frac{8}{25} \times \frac{100}{\frac{R}{2}}$$

$$\Rightarrow R^2 = \frac{8 \times 200}{25} = 64$$

$$\Rightarrow R = \sqrt{64} = 8\% \text{ per annum}$$

60. (c) $m + \frac{1}{m-2} = 4$

$$\Rightarrow m + \frac{1}{m-2} - 2 = 4 - 2$$

$$\Rightarrow (m-2) + \frac{1}{(m-2)} = 4 - 2 = 2$$

On squaring both sides,

$$(m-2)^2 + \frac{1}{(m-2)^2} + 2(m-2)\left(\frac{1}{m-2}\right) = 4$$

$$\Rightarrow (m-2)^2 + \frac{1}{(m-2)^2} = 4 - 2 = 2$$

61. (a) $\frac{x}{b+c} = \frac{y}{c+a}$

$$= \frac{x-y}{b+c-c-a} = \frac{x-y}{b-a}; \quad \frac{y}{c+a} = \frac{z}{a+b}$$

$$= \frac{y-z}{c+a-a-b} = \frac{y-z}{c-b}; \quad \frac{z}{a+b} = \frac{x}{b+c}$$

$$= \frac{z-x}{a+b-b-c} = \frac{z-x}{a-c}$$

$$\therefore \frac{x-y}{b-a} = \frac{y-z}{c-b} = \frac{z-x}{a-c}$$

প্র্যাক্টিস

প্র্যাক্টিস

প্র্যাক্টিস

62. (a) $x^2 + y^2 - z^2 + 2xy$
 $= x^2 + y^2 + 2xy - z^2$
 $= (x+y)^2 - z^2 = (x+y+z)(x+y-z)$
 $= (b+c-2a+c+a-2b+a+b-2c)(x+y-z) = 0$

63. (d) Check through options.

If $x = y = z$, then

প্র্যাক্টিস

$$\frac{1}{x^2} + \frac{1}{y^2} + \frac{1}{z^2} = \frac{3}{x^2} \text{ and } \frac{1}{xy} + \frac{1}{yz} + \frac{1}{zx}$$

$$= \frac{1}{x^2} + \frac{1}{x^2} + \frac{1}{x^2} = \frac{3}{x^2}$$

64. (a) $\frac{2\sin\theta - \cos\theta}{\cos\theta + \sin\theta} = 1$

Dividing numerator and denominator by $\sin\theta$,

$$\frac{2 - \cot\theta}{\cot\theta + 1} = 1$$

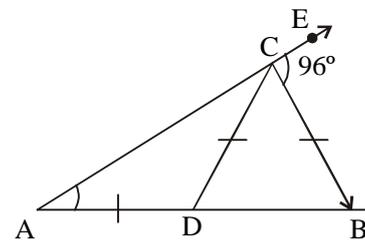
$$\Rightarrow 2 - \cot\theta = \cot\theta + 1$$

$$\Rightarrow 2\cot\theta = 1$$

$$\Rightarrow \cot\theta = \frac{1}{2}$$

প্র্যাক্টিস

65. (c)



Let $\angle ACD = a = \angle DAC$

$\therefore \angle CDB = 2a = \angle CBD$

The angles of the base of an isosceles triangle are equal.

$$\therefore \angle ACB = 180^\circ - 96^\circ = 84^\circ$$

$$\Rightarrow \angle ACD + \angle DCB = 84^\circ$$

$$\Rightarrow a + 180^\circ - 4a = 84^\circ$$

$$\Rightarrow 180^\circ - 3a = 84^\circ$$

$$\Rightarrow 3a = 180^\circ - 84^\circ = 96^\circ$$

প্র্যাক্টিস

$$\Rightarrow a = \frac{96}{3} = 32^\circ$$

$$\Rightarrow \angle DBC = 2a = 64^\circ$$

66. (c) We know that

$$a^3 + b^3 + c^3 - 3abc$$

$$= (a+b+c)(a^2 + b^2 + c^2 - ab - bc - ca)$$

$$= \frac{1}{2}(a+b+c)[(a-b)^2 + (b-c)^2 + (c-a)^2]$$

$$\begin{aligned} &\therefore \sqrt[3]{(333)^3 + (333)^3 + (334)^3} \\ &\quad - \sqrt[3]{-3 \times 333 \times 333 \times 334} \\ &\Rightarrow \sqrt[3]{\frac{1}{2}(333+333+334)[(333-333)^2} \\ &\quad + (333-334)^2 + (334-333)^2]} \text{ প্র্যাচিভর্স} \\ &= \sqrt[3]{\frac{1}{2} \times 1000 \times 2} = \sqrt[3]{1000} \\ &= \sqrt[3]{10 \times 10 \times 10} = 10 \end{aligned}$$

67. (b) $a = \sqrt{2} + 1$
 $\therefore a + 1 = \sqrt{2} + 2$
 Again, $b = \sqrt{2} - 1$
 $\therefore b + 1 = \sqrt{2} - 1 + 1 = \sqrt{2}$
 $\therefore \frac{1}{a+1} + \frac{1}{b+1}$
 $= \frac{1}{\sqrt{2}+2} + \frac{1}{\sqrt{2}}$
 $= \frac{\sqrt{2} + \sqrt{2} + 2}{\sqrt{2}(\sqrt{2}+2)} = \frac{2+2\sqrt{2}}{2+2\sqrt{2}} = 1$

68. (c) $\frac{x}{y} = \frac{4}{5}$ (Given)
 Expression $= \frac{4}{7} + \frac{2y-x}{2y+x}$
 $= \frac{4}{7} + \frac{\frac{2y-x}{y}}{\frac{2y+x}{y}}$
 $= \frac{4}{7} + \frac{2-\frac{x}{y}}{2+\frac{x}{y}} = \frac{4}{7} + \frac{2-\frac{4}{5}}{2+\frac{4}{5}}$
 $= \frac{4}{7} + \frac{\frac{10-4}{5}}{\frac{10+4}{5}} = \frac{4}{7} + \frac{6}{14}$
 $= \frac{4}{7} + \frac{3}{7} = \frac{7}{7} = 1$

69. (c) $2x = \sqrt{a} + \frac{1}{\sqrt{a}}$
 On squaring both sides,
 $4x^2 = a + \frac{1}{a} + 2$
 $\Rightarrow 4x^2 - 4 = a + \frac{1}{a} + 2 - 4$ প্র্যাচিভর্স
 $= a + \frac{1}{a} - 2$
 $\therefore \sqrt{4x^2 - 4} = \sqrt{\left(\sqrt{a} - \frac{1}{\sqrt{a}}\right)^2}$
 $= \sqrt{a} - \frac{1}{\sqrt{a}}$
 $\therefore \sqrt{x^2 - 1} = \frac{1}{2} \left(\sqrt{a} - \frac{1}{\sqrt{a}}\right)$
 $\therefore \text{Expression} = \frac{\sqrt{x^2 - 1}}{x - \sqrt{x^2 - 1}}$ প্র্যাচিভর্স
 $= \frac{\frac{1}{2} \left(\sqrt{a} - \frac{1}{\sqrt{a}}\right)}{\frac{1}{2} \left(\sqrt{a} + \frac{1}{\sqrt{a}}\right) - \frac{1}{2} \left(\sqrt{a} - \frac{1}{\sqrt{a}}\right)}$
 $= \frac{\frac{1}{2} \left(\sqrt{a} - \frac{1}{\sqrt{a}}\right)}{\frac{1}{2} \left(\sqrt{a} - \frac{1}{\sqrt{a}}\right)} = \frac{1}{2} \sqrt{a} \left(\sqrt{a} - \frac{1}{\sqrt{a}}\right)$
 $= \frac{1}{2} (a - 1)$

70. (d) $a + \frac{1}{b} = b + \frac{1}{c} = c + \frac{1}{a}$ প্র্যাচিভর্স
 $\Rightarrow \frac{abc+c}{bc} = \frac{abc+a}{ac} = \frac{abc+b}{ab}$
 $\Rightarrow \frac{c}{bc} = \frac{a}{ac} = \frac{b}{ab}$
 $\Rightarrow \frac{1}{b} = \frac{1}{c} = \frac{1}{a}$
 $\Rightarrow a = b = c = 1$
 $\therefore a^2 b^2 c^2 = 1$

71. (d) Expression

$$\begin{aligned}
 &= \sqrt{\frac{1+\sin\theta}{1-\sin\theta}} + \sqrt{\frac{1-\sin\theta}{1+\sin\theta}} && \text{শ্রুতিভঙ্গি} \\
 &= \sqrt{\frac{(1+\sin\theta)(1+\sin\theta)}{(1-\sin\theta)(1+\sin\theta)}} + \sqrt{\frac{(1-\sin\theta)(1-\sin\theta)}{(1+\sin\theta)(1-\sin\theta)}} \\
 &= \sqrt{\frac{(1+\sin\theta)^2}{1-\sin^2\theta}} + \sqrt{\frac{(1-\sin\theta)^2}{1-\sin^2\theta}} \\
 &= \sqrt{\frac{(1+\sin\theta)^2}{\cos^2\theta}} + \sqrt{\frac{(1-\sin\theta)^2}{\cos^2\theta}} \\
 &= \frac{1+\sin\theta}{\cos\theta} + \frac{1-\sin\theta}{\cos\theta} \\
 &= \frac{1+\sin\theta+1-\sin\theta}{\cos\theta} = \frac{2}{\cos\theta} && \text{শ্রুতিভঙ্গি} \\
 &= 2\sec\theta
 \end{aligned}$$

72. (c) Let A and B have ₹2x and ₹x initially.

$$\begin{aligned}
 \therefore 2x-2 &= x+2 \\
 \Rightarrow x &= 4 \\
 \therefore \text{Initial amount with A} &= ₹8 \\
 \therefore \text{Initial amount with B} &= ₹4.
 \end{aligned}$$

73. (d) Using Rule 9,
Required increase percent

$$\begin{aligned}
 &= \frac{40}{100-40} \times 100 \\
 &= \frac{40}{60} \times 100 = \frac{200}{3} = 66\frac{2}{3}\%
 \end{aligned}$$

74. (c) Let the C.P. of article be ₹x, then

$$\begin{aligned}
 \frac{120x}{100} - \frac{115x}{100} &= 27 \\
 \Rightarrow \frac{5x}{100} &= 27 && \text{শ্রুতিভঙ্গি} \\
 \Rightarrow x &= \frac{27 \times 100}{5} = ₹540
 \end{aligned}$$

75. (b) Amount after 10 years

$$\begin{aligned}
 &= P\left(1 + \frac{RT}{100}\right) = P\left(1 + \frac{R \times 10}{100}\right) \\
 &= ₹P\left(1 + \frac{R}{10}\right) \\
 \therefore \text{Interest} &= ₹P\left(1 + \frac{R}{10}\right) \times \frac{2}{5}
 \end{aligned}$$

$$\therefore \text{Rate} = \frac{\text{S.I.} \times 100}{\text{Principal} \times \text{Time}}$$

$$\Rightarrow R = \frac{P\left(1 + \frac{R}{10}\right) \times \frac{2}{5} \times 100}{P \times 10} && \text{শ্রুতিভঙ্গি}$$

$$\Rightarrow R = 4\left(1 + \frac{R}{10}\right)$$

$$\Rightarrow \frac{R}{4} = 1 + \frac{R}{10}$$

$$\Rightarrow \frac{R}{4} - \frac{R}{10} = 1$$

$$\Rightarrow \frac{5R - 2R}{20} = 1$$

$$\Rightarrow 3R = 20$$

$$\Rightarrow R = \frac{20}{3} = 6\frac{2}{3}\%$$

76. (d) Principal = P (let)

$$\therefore \text{C.I.} = P\left[\left(1 + \frac{R}{100}\right)^T - 1\right]$$

$$\Rightarrow 510 = P\left[\left(1 + \frac{25}{200}\right)^2 - 1\right]$$

$$\Rightarrow 510 = P\left[\left(1 + \frac{1}{8}\right)^2 - 1\right]$$

$$\Rightarrow 510 = P\left[\left(\frac{9}{8}\right)^2 - 1\right]$$

$$\Rightarrow 510 = P\left(\frac{81}{64} - 1\right)$$

$$\Rightarrow 510 = P\left(\frac{81-64}{64}\right) && \text{শ্রুতিভঙ্গি}$$

$$\Rightarrow 510 = \frac{17P}{64}$$

$$\Rightarrow P = \frac{510 \times 64}{17} = ₹1920$$

$$\therefore \text{S.I.} = \frac{\text{Principal} \times \text{Time} \times \text{Rate}}{100}$$

$$= \frac{1920 \times 2 \times 25}{100 \times 2} = ₹480$$

$$77. (b) \frac{3a+4b}{3c+4d} = \frac{3a-4b}{3c-4d}$$

$$\Rightarrow \frac{3a+4b}{3a-4b} = \frac{3c+4d}{3c-4d}$$

By Componendo and Dvidendo

$$\frac{3a+4b+3a-4b}{3a+4b-3a+4b}$$

$$= \frac{3c+4d+3c-4d}{3c+4d-3c+4d}$$

$$\Rightarrow \frac{6a}{8b} = \frac{6c}{8d}$$

$$\Rightarrow \frac{a}{b} = \frac{c}{d}$$

$$\Rightarrow ad = bc$$

$$78. (a) 2x - \frac{1}{2x} = 5$$

On dividing by 2,

$$x - \frac{1}{4x} = \frac{5}{2}$$

On squaring both sides

$$\left(x - \frac{1}{4x}\right)^2 = \left(\frac{5}{2}\right)^2 = \frac{25}{4}$$

$$\Rightarrow x^2 + \frac{1}{16x^2} - 2 \times x \times \frac{1}{4x} = \frac{25}{4}$$

$$\Rightarrow x^2 + \frac{1}{16x^2} = \frac{25}{4} + \frac{1}{2}$$

$$= \frac{25+2}{4} = \frac{27}{4}$$

$$\Rightarrow x^2 + \frac{1}{16x^2} - 2$$

$$= \frac{27}{4} - 2 = \frac{27-8}{4} = \frac{19}{4}$$

$$79. (c) p^2 + \frac{1}{p^2} = 47$$

$$\Rightarrow \left(p + \frac{1}{p}\right)^2 - 2 = 47$$

$$\Rightarrow \left(p + \frac{1}{p}\right)^2 = 47 + 2 = 49$$

$$\Rightarrow p + \frac{1}{p} = \sqrt{49} = 7$$

80. (b) Using Rule 8,

$$2p + \frac{1}{p} = 4$$

$$\Rightarrow p + \frac{1}{2p} = 2$$

$$\therefore \left(p + \frac{1}{2p}\right)^3$$

$$= p^3 + \frac{1}{8p^3} + 3 \cdot p \cdot \frac{1}{2p} \left(p + \frac{1}{2p}\right)$$

$$\Rightarrow 8 = p^3 + \frac{1}{8p^3} + \frac{3}{2} \times 2$$

$$\Rightarrow p^3 + \frac{1}{8p^3} = 8 - 3 = 5$$

81. (b) Successful boys in English or Maths or both

$$= 80 + 85 - 75 = 90\%$$

Unsuccessful boys = 10%

\therefore Total number of boys

$$= \frac{100}{10} \times 45 = 450$$

82. (c) Let the C.P. of bucket be ₹x.

According to the question,

$$\frac{108x}{100} - \frac{92x}{100} = 28$$

$$\Rightarrow \frac{16x}{100} = 28$$

$$\Rightarrow x = \frac{28 \times 100}{16} = ₹175$$

83. (d) Required ratio = $5 : \frac{2}{5} = 25 : 2$

$$\frac{\text{loan amount}}{\text{Interest amount}} = \frac{5}{2}$$

$$\Rightarrow \text{Interest rate} = \frac{2}{5}$$

$$\left[\because \frac{P+I}{I} = \frac{5}{2} \Rightarrow \frac{P}{I} + 1 = \frac{5}{2} \right]$$

$$\Rightarrow \frac{P}{I} = \frac{3}{2}, \text{ then } I = \frac{2}{5}$$

প্র্যাচিভার্স

$$\frac{\text{loan amount}}{\text{Interest rate}} = \frac{5}{2/5} = \frac{25}{2} \text{ or } 25 : 2$$

84. (c) Using Rule 6,

$$\text{Time} = \frac{3}{2} \times 2 = 3 \text{ half years}$$

$$\text{Rate} = \frac{10}{2} = 5\% \text{ per half years}$$

[\therefore when $r \rightarrow r/2$, then $t \rightarrow 2t$]

Difference

$$= P \left(\frac{r^3}{1000000} + \frac{3r^2}{10000} \right)$$

$$\Rightarrow 244 = P \left(\frac{125}{1000000} + \frac{75}{10000} \right)$$

প্র্যাচিভার্স

$$\Rightarrow 244 = P \left(\frac{7625}{1000000} \right)$$

$$\Rightarrow P = \frac{244 \times 1000000}{7625} = ₹ 32000$$

85. (b) $x + \frac{1}{x} = 2$

$$\Rightarrow x^2 + 1 = 2x \Rightarrow x^2 - 2x + 1 = 0$$

$$\Rightarrow (x - 1)^2 = 0$$

$$\Rightarrow x = 1$$

$$\therefore x^2 + \frac{1}{x^3} = 1 + 1 = 2$$

86. (b) $(a^2 + b^2)^3 = (a^3 + b^3)^2$

$$\Rightarrow a^6 + b^6 + 3a^2b^2(a^2 + b^2)$$

$$= a^6 + b^6 + 2a^3b^3$$

$$\Rightarrow 3(a^2 + b^2) = 2ab$$

$$\Rightarrow \frac{a^2 + b^2}{ab} = \frac{2}{3}$$

$$\Rightarrow \frac{a}{b} + \frac{b}{a} = \frac{2}{3}$$

87. (c) $x + \frac{1}{x} = 2$

$$\Rightarrow x^2 - 2x + 1 = 0$$

$$\Rightarrow (x - 1)^2 = 0 \Rightarrow x = 1$$

$$\therefore x^{17} + \frac{1}{x^{19}} = 1 + 1 = 2$$

88. (b) $3x + \frac{3}{x} = 1$

$$\Rightarrow x + \frac{1}{x} = \frac{1}{3}$$

প্র্যাচিভার্স

On cubing both sides,

$$x^3 + \frac{1}{x^3} + 3 \left(x + \frac{1}{x} \right) = \frac{1}{27}$$

$$\Rightarrow x^3 + \frac{1}{x^3} + 3 \times \frac{1}{3} = \frac{1}{27}$$

$$\Rightarrow x^3 + \frac{1}{x^3} + 1 = \frac{1}{27}$$

89. (c) Let the C.P. of A be ₹ x, then

$$\frac{x \times 125}{100} \times \frac{90}{100} = 675$$

$$\Rightarrow x = \frac{675 \times 100 \times 100}{125 \times 90} = ₹ 600$$

প্র্যাচিভার্স

90. (d) $A = P \left(I + \frac{R}{100} \right)^T$

$$\Rightarrow 1.44 = P \left(I + \frac{R}{100} \right)^2$$

$$\Rightarrow (1.2)^2 = \left(I + \frac{R}{100} \right)^2$$

$$\Rightarrow I + \frac{R}{100} = 1.2$$

$$\Rightarrow R = 0.2 \times 100 = 20\%$$

91. (d) $x + \frac{1}{x} = 2$

$$\Rightarrow x^2 + 1 = 2x$$

$$\Rightarrow x^2 - 2x + 1 = 0$$

$$\Rightarrow (x - 1)^2 = 0 \Rightarrow x = 1$$

$$\therefore x^{2013} + \frac{2}{x^{2014}} = 1 + 1 = 2$$

প্র্যাচিভার্স

92. (c) Expression

$$= \frac{3}{15} a^5 b^6 c^3 \times \frac{5}{9} ab^5 c^4$$

$$= \frac{10}{27} a^2 bc^3$$

$$= \left(\frac{3}{15} \times \frac{5}{9} \times \frac{27}{10} \right) \left(\frac{a^6 b^{11} c^7}{a^2 bc^3} \right)$$

$$= \frac{3}{10} a^{6-2} b^{11-1} c^{7-3}$$

$$= \frac{3}{10} a^4 b^{10} c^4 \quad \left[\begin{array}{l} \because a^m \times a^n = a^{m+n} \\ a^m \div a^n = a^{m-n} \end{array} \right]$$

93. (c) $\frac{x^3 + 3y^2x + y^3 + 3x^2y}{x^3 + 3y^2x - y^3 - 3x^2y}$

$$= \frac{35 + 19}{35 - 19} = \frac{54}{16}$$

$$\Rightarrow \frac{(x+y)^3}{(x-y)^3} = \frac{27}{8} = \left(\frac{3}{2}\right)^3$$

$$\Rightarrow \frac{x+y}{x-y} = \frac{3}{2}$$

By componendo and dividendo again

$$\frac{x+y+x-y}{x+y-x+y} = \frac{3+2}{3-2} \Rightarrow \frac{x}{y} = 5$$

94. (b) Total profit in sales

$$= ₹ \left(\frac{750 \times 6}{100} - \frac{750 \times 4}{100} \right)$$

$$= \text{Rs. } (45 - 30) = \text{Rs. } 15$$

$$\left[\begin{array}{l} \text{or, Profit} = (6-4)\% \text{ of } 750 \\ = \frac{750 \times 2}{100} = ₹ 15 \end{array} \right]$$

$$\therefore \text{Profit per cent} = \frac{15}{1500} \times 100 = 1\%$$

95. (c) Putting $x = 2$ in the equation

$$2x + y = 6,$$

$$2 \times 2 + y = 6$$

$$\Rightarrow y = 6 - 4 = 2$$

\therefore Required point = (2, 2)

96. (c) On putting $y = -x$ in the equation

$$5y + 7x = 24,$$

$$-5x + 7x = 24$$

$$\Rightarrow 2x = 24 \Rightarrow x = 12$$

$$\& y = -12$$

$$\therefore m = x = 12, n = y = -12$$

$$\Rightarrow m + n = 12 - 12 = 0$$

97. (a) $a : b = 7 : 9$

$$b : c = 3 : 5 = 9 : 15$$

$$\therefore a : b : c = 7 : 9 : 15$$

98. (c) $\frac{x}{y} = \frac{3}{4}$ (Given)

$$\therefore \frac{5x-2y}{7x+2y} = \frac{5\frac{x}{y}-2}{7\frac{x}{y}+2}$$

$$= \frac{5 \times \frac{3}{4} - 2}{7 \times \frac{3}{4} + 2} = \frac{\frac{15-8}{4}}{\frac{21+8}{4}} = \frac{7}{29}$$

99. (c) $x = \sqrt[3]{a + \sqrt{a^2 + b^3}} + \sqrt[3]{a - \sqrt{a^2 + b^3}}$

Cubing both sides,

$$x^3 = \left(\sqrt[3]{a + \sqrt{a^2 + b^3}} \right)^3 + \left(\sqrt[3]{a - \sqrt{a^2 + b^3}} \right)^3$$

$$+ 3 \left(\sqrt[3]{a + \sqrt{a^2 + b^3}} \right)$$

$$\left(\sqrt[3]{a - \sqrt{a^2 + b^3}} \right) \left(\sqrt[3]{a + \sqrt{a^2 + b^3}} + \sqrt[3]{a - \sqrt{a^2 + b^3}} \right)$$

$$= a + \sqrt{a^2 + b^3} + a - \sqrt{a^2 + b^3}$$

$$+ 3 \left(a + \sqrt{a^2 + b^3} \right)^{\frac{1}{3}} \left(a - \sqrt{a^2 + b^3} \right)^{\frac{1}{3}} x$$

$$= 2a + 3(a^2 - b^3)^{\frac{1}{3}} x$$

$$= 2a + (-3bx)$$

$$\therefore x^3 + 3bx = 2a$$

100. (a) Let the income of A, B and C be ₹3x, ₹7x and ₹4x respectively and their expenses be ₹4y, ₹3y and ₹5y respectively.

$$\therefore 3x = 2400$$

$$\Rightarrow x = 800$$

$$\therefore 4y = 2400 - 300 = 2100$$

$$\Rightarrow y = 525$$

$$\therefore \text{B's saving} = (7x - 3y)$$

$$= ₹(7 \times 800 - 3 \times 525)$$

$$= ₹(5600 - 1575) = ₹4025$$

$$\text{and C's savings} = ₹(4x - 5y)$$

$$= (3200 - 2625) = ₹575$$